

ASTRONOMY 9: HISTORY OF COSMOLOGY
Handout #21

J. E. Baker
UC Berkeley, Spring 2000

Life in the Quantum World

- The Nature of Light Revisited
 - Recall the “ultraviolet catastrophe”: classical physics predicts blackbody spectrum keeps rising, infinite energies at high frequencies!
 - Max **Planck** (1900) makes a desperate hypothesis to explain the observed spectra:
 - Matter can only absorb and emit light in discrete (*quantized*) amounts:

$$E = hf$$

- Light of frequency f comes in indivisible little packets of energy hf
- $h \approx 6.627 \times 10^{-34}$ Joule sec is Planck’s constant
 - * Joule is an amount of energy (about enough to lift your textbook a few cm)
 - * Small size of h means we don’t usually see weird quantum effects in everyday life
- Einstein (1905) studies *photoelectric effect*
 - * Awarded 1921 Nobel prize for this work (not relativity!)
 - * Shine light of frequency f on a metal
 - * No electrons are ejected for $f < f_0$
 - * For $f > f_0$, energy of ejected electrons is $h(f - f_0)$
 - * Light is behaving like a *particle* (**photon**)
- But sometimes light behaves like a wave (eg, it diffracts around corners) \Rightarrow **wave/particle duality**
- The Nature of Matter: A Brief History of Atomic Theory
 - J. J. Thompson (\sim 1900): “plum pudding” model
 - * Electrons are plums
 - * Diffuse positively charged pudding
 - Ernest Rutherford (1911)
 - * Studies “Rutherford scattering” of charged particles hitting thin metal sheets
 - * Almost all are just slightly deflected, but a few bounce straight back
 - * Atomic nucleus is small and very dense, most of atom is empty space!
 - * Electrons whiz around
 - Niels Bohr (1913)
 - * Electron is *accelerating* as it moves around nucleus
 - * Maxwell’s equations say it should radiate all its energy and collapse to the nucleus!
 - * Bohr’s solution: electron can only exist in *discrete* atomic levels—atoms are quantized too!
 - * Light is emitted or absorbed when electron jumps between levels (a “quantum leap”: it doesn’t go in between)
 - * Each atom has a different set of levels, explains **spectral lines**
 - Louis de Broglie (1924)
 - * Just as light can behave like particles, electrons can behave like waves!
 - * Electron can exist only in orbits where integer number of waves “fit” around the orbit
 - * Explains Bohr’s quantization idea
- The Uncertainty Principle
 - Werner Heisenberg (1925)

- If precisely measure momentum (p) of a particle, its position (x) becomes completely uncertain, and vice versa!

$$\Delta x \Delta p > \frac{\hbar}{2}$$

where $\hbar = h/2\pi$ and Δ means “uncertainty in”

- Can also be expressed as relationship between measurements of energy and time: $\Delta E \Delta t > \hbar/2$
 - Destroys old Laplacian philosophy of *determinism*!
 - Observer also plays a crucial role: what you choose to measure influences the physical state of the system!
- Max Born and Erwin Schrödinger (1927)
 - Quantum mechanics (QM) only describes *probabilities*
 - The **wavefunction** ψ specifies all there is to know about a system
 - Schrodinger equation determines evolution of wavefunction in time and space
 - The wavefunction of an electron at point x represents the probability of finding it at x : $P \propto |\psi|^2$
 - Particles are “fuzzy”!
 - Quantum Statistics
 - Particles have an intrinsic “spin”, also quantized: only comes in units of $\hbar/2$
 - Particles aren’t really little spheres, spin is not really like our common-sense notion
 - Two types of particles, classified according to spin:
 - **Fermions**: Spins are a half-integer multiple ($1/2, 3/2, 5/2, \dots$) of \hbar
 - * Named after Enrico Fermi (nuclear physicist)
 - * Examples: electron, proton, neutron (normal matter)
 - * “Anti-social” particles: obey Pauli’s Exclusion Principle
 - * No two fermions may be in the same quantum state
 - **Bosons**: Spins are an integer multiple ($0, 1, 2, \dots$) of \hbar
 - * Named after Satyendranath Bose (Indian physicist)
 - * Examples: photon (spin-0), graviton (spin-2, carries gravitational force just like photon carries electromagnetism)
 - * Gregarious, “social” particles: all like to enter the same quantum state!
 - * Note: spin-2 in a sense means you have to rotate by $2 \times 360^\circ = 720^\circ$ before you look the same! Spin-1/2 means you only have to rotate by 180°
 - Interpretation of Quantum Mechanics
 - Quantum mechanics *works* very well, in that it is a great tool for calculating things
 - Problems only arise when you try to *interpret* it in terms of our everyday experience
 - Very disturbing to many founders of quantum physics
 - Recent research is beginning to explore boundary between quantum and classical realms: how does quantum weirdness give way to macroscopic classical normality?
 - 1. Copenhagen (“standard”) interpretation (Bohr and others, 1920s)
 - Act of observation mysteriously “collapses the wavefunction”
 - When you’re not looking at it, the electron spreads out all over space, and different outcomes are superposed on top of each other
 - The act of observation somehow localizes things, or selects a particular outcome
 - Einstein objects: do you really think the Moon isn’t there when you’re not looking at it?
 - Example: Schrodinger’s cat
 - * Feline in a box with vial of poison, decay of a radioactive atom triggers release of poison
 - * QM says the atom enters a “superposition of states”, both decayed and non-decayed, until an observation is made
 - * But then is the cat also simultaneously dead and not-dead? Implies macroscopic manifestation of quantum weirdness
 - * What exactly is the act of “observation”? Does human consciousness play a special physical role? Or do common environmental interactions collapse the wavefunction and prevent the cat from entering superposition?

2. Many-worlds interpretation (Hugh Everett, 1957)
 - *All* possibilities embodied by the wavefunction *actually occur!*
 - Universe constantly forks into a multitude of different versions of itself (“parallel universes”)
 - In one universe, Schrodinger’s cat is alive; in another it is dead
 - Universes are cut off from each other
3. “Hidden variables” (historically favored by Einstein and others)
 - Idea: QM is a terribly incomplete theory, does not preserve *locality*
 - Example: Einstein-Podolsky-Rosen (EPR) “paradox”
 - * Send two particles off in a quantum superposition (eg, spins of each are pointing both up and down at the same time!)
 - * Measurement of one particle causes it to choose one state or the other
 - * Has instantaneous effect on the other particle, even if it has traveled half-way across the universe! Spooky
 - * Note: doesn’t violate special relativity, since still can’t send a *signal* faster than light
 - Some unknown underlying “variables” affect the system, allow only local effects
 - Experimental evidence does not support this interpretation